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## Logarithmic Amp. and Exponential Amp.

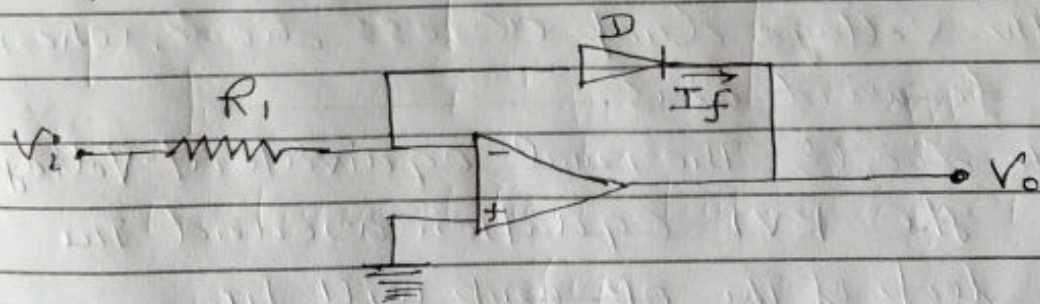


The electronic circuits which perform the mathematical operations such as logarithmic & exponential with an amplification are called as Logarithmic amp. and exponential (Antilogarithmic) Amp. respectively.

### Logarithmic Amplifier:

A logarithmic amp. or a log amp. is an electronic circuit that produces an output that is proportional to the logarithm of the applied input. This section discusses about the op-amp. based logarithmic amplifier in detail.

An op-amp. based logarithmic amp. produces a voltage at the output, which is proportional to the logarithm of the voltage applied to the resistor connected to its inverting terminal. The circuit diagram of an op-amp. based logarithmic amp. is shown in the following figure.



In the above circuit, the non-inverting input terminal of the op-amp. is connected



to ground. That means Zero Volts is applied at the non-inverting input-terminal of the OP-amp.

According to the Virtual Short concept, the voltage at the inverting input terminal of an OP-amp will be equal to the voltage at its non-inverting input terminal. So, the voltage at the inverting input terminal will be Zero Volts.

The nodal equation at the inverting input terminal's node is -

$$\frac{0 - V_i}{R_1} + I_f = 0$$

$$\Rightarrow I_f = V_i / R_1 \quad \text{--- (1)}$$

The following is the equation for current flowing through a diode, when it is in forward bias

$$I_f = I_s e^{(V_f / nVT)} \quad \text{--- (2)}$$

- $I_s$ , is the saturation current of the diode.
- $V_f$ , is the voltage drop across diode, when it is in forward bias.
- $V_T$ , is the diode's thermal equivalent voltage.

The KVL equation around the feedback loop of the OP-amp will be

$$0 - V_f - V_o = 0$$

$$\Rightarrow V_f = -V_o$$



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Substituting the value of  $V_f$  in equation (2),

we get 
$$I_f = I_s e^{(-V_o/nVT)} \quad \text{--- (3)}$$

observe that the left hand side terms of both eqn (1) and (3) are same.

Hence, equate the right hand side term of those two equations as shown below —

$$\frac{V_i}{R_1} = I_s e^{(-V_o/nVT)}$$

$$\frac{V_i}{R_1 I_s} = e^{(-V_o/nVT)}$$

Applying natural logarithm on both sides, we get,

$$\ln\left(\frac{V_i}{R_1 I_s}\right) = \frac{-V_o}{nVT}$$

$$V_o = -nVT \ln\left(\frac{V_i}{R_1 I_s}\right)$$

Note that in the above equation, the parameters  $n$ ,  $V_T$  and  $I_s$  are constants, so, the output voltage  $V_o$  will be proportional to the natural logarithm of the input voltage  $V_i$ , for a fixed value of resistance  $R_1$ .

Therefore, the OP-amp. based logarithmic amp. circuit discussed above will produce on output, which is proportional to the natural logarithm of the input voltage.



$V_T$  when  $R_1 I_S = 1V$ .

Observe that the output voltage

$V_o$  has a -ve sign, which indicates that there exists a  $180^\circ$  phase difference between the input and the output.



Logarithmic Amplifier :-